#### EE382V: Principles in Computer Architecture Parallelism and Locality Fall 2008 Lecture 9 – Example of Using Parallel Constructs

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- Finish discussion of patterns
- Molecular dynamics example
  - Problem description
  - Steps to solution
    - Build data structures; Compute forces; Integrate for new; positions; Check global solution; Repeat
  - Finding concurrency
    - Scans; data decomposition; reductions
  - Algorithm structure
  - Supporting structures

# **Patterns for Parallelizing Programs**

#### 4 Design Spaces

#### **Algorithm Expression**

- Finding Concurrency
  - Expose concurrent tasks
- Algorithm Structure
  - Map tasks to processes to exploit parallel architecture

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#### **Software Construction**

- Supporting Structures
  - Code and data structuring patterns
- Implementation Mechanisms
  - Low level mechanisms used to write parallel programs



### ILP, DLP, and TLP in SW and HW

- ILP
  - 000
  - Dataflow
  - VLIW
- DLP
  - SIMD
  - Vector
- TLP
  - Essentially multiple cores with multiple sequencers

- ILP
  - Within straight-line code
- DLP
  - Parallel loops
  - Tasks operating on disjoint data
    - No dependencies within parallelism phase
- TLP
  - All of DLP +
  - Producer-consumer chains



## ILP, DLP, and TLP and Supporting Patterns

	Task parallelism	Divide and conquer	Geometric decomposition	Recursive data	Pipeline	Event-based coordination
ILP						
DLP						
TLP						

# ILP, DLP, and TLP and Supporting Patterns

	Task parallelism	Divide and conquer	Geometric decomposition	Recursive data	Pipeline	Event-based coordination
ILP	inline / unroll	inline	unroll	inline	inline / unroll	inline
DLP	natural or local- conditions	after enough divisions	natural	after enough branches	difficult	local- conditions
TLP	natural	natural	natural	natural	natural	natural

ST.

# ILP, DLP, and TLP and Implementation Patterns

	SPMD	Loop Parallelism	Mater/Worker	Fork/Join
ILP				
DLP				
TLP				

### ILP, DLP, and TLP and Implementation Patterns

	SPMD	Loop Parallelism	Mater/Worker	Fork/Join
ILP	pipeline	unroll	inline	inline
DLP	natural or local- conditional	natural	local-conditional	after enough divisions + local-conditional
TLP	natural	natural	natural	natural



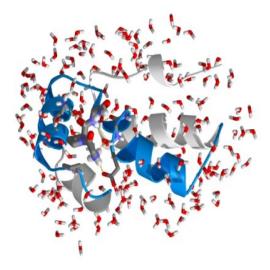
- Molecular dynamics example
  - Problem description
  - Steps to solution
    - Build data structures; Compute forces; Integrate for new; positions; Check global solution; Repeat
  - Finding concurrency
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  - Algorithm structure
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- Parallel Scan slides courtesy David Kirk (NVIDIA) and Wen-Mei Hwu (UIUC)
  - Taken from EE493-AI taught at UIUC in Sprig 2007
- Reduction slides courtesy Dr. Rodric Rabbah (IBM)
  - Taken from 6.189 IAP taught at MIT in 2007



- Highly optimized molecular-dynamics package
  - Popular code
  - Specifically tuned for protein folding
  - Hand optimized loops for SSE3 (and other extensions)

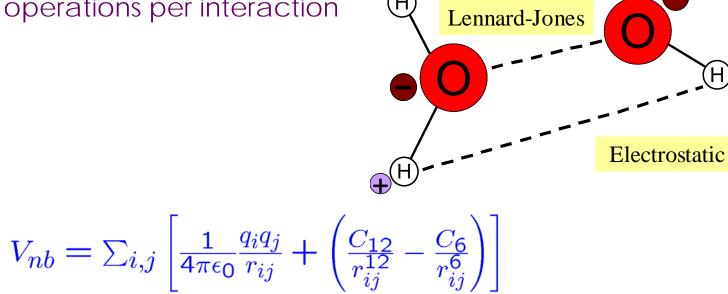


# **Gromacs Components**

- Non-bonded forces
  - Water-water with cutoff
  - Protein-protein tabulated
  - Water-water tabulated
  - Protein-water tabulated
- Bonded forces
  - Angles
  - Dihedrals
- Boundary conditions
- Verlet integrator
- Constraints
  - SHAKE
  - SETTLE
- Other
  - Temperature-pressure coupling
  - Virial calculation

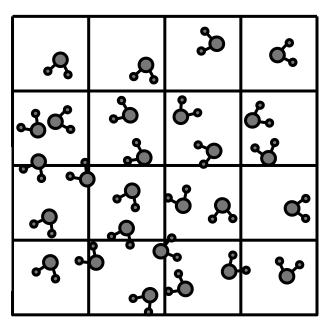
### **GROMACS** Water-Water Force Calculation

- Non-bonded long-range interactions
  - Coulomb
  - Lennard-Jones
  - 234 operations per interaction

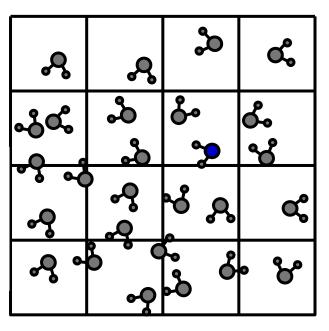


#### Water-water interaction ~75% of GROMACS run-time

- Full non-bonded force calculation is o(n<sup>2</sup>)
- GROMACS approximates with a cutoff
  - Molecules located more than r<sub>c</sub> apart do not interact
  - $O(nr_c^{3})$



- Full non-bonded force calculation is *o(n<sup>2</sup>)*
- GROMACS approximates with a cutoff
  - Molecules located more than r<sub>c</sub> apart do not interact
  - $O(nr_c^{3})$



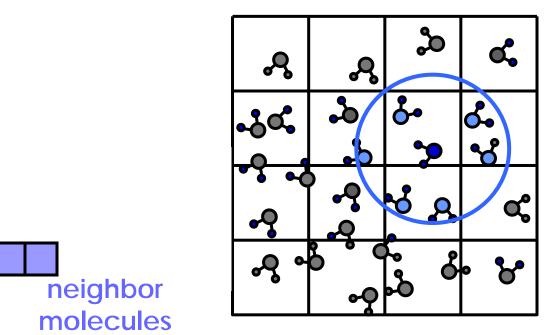




- Full non-bonded force calculation is o(n<sup>2</sup>)
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centra

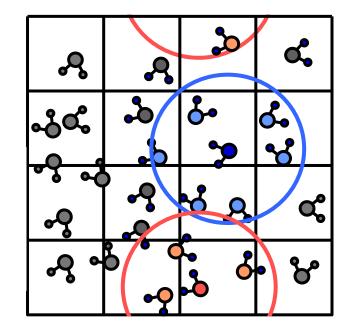
molecules



- Full non-bonded force calculation is o(n<sup>2</sup>)
- GROMACS approximates with a cutoff
  - Molecules located more than r<sub>c</sub> apart do not interact
  - O(nr<sub>c</sub><sup>3</sup>)

central

molecules

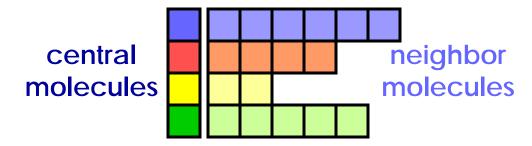


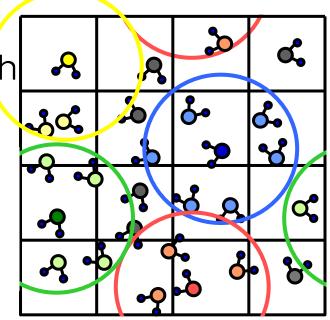


neighbor

molecules

- Full non-bonded force calculation is o(n<sup>2</sup>)
- GROMACS approximates with a cutoff
  - Molecules located more than r<sub>c</sub> apart do not interact
  - $O(nr_c^{3})$
- Separate neighbor-list for each molecule
  - Neighbor-lists have variable number of elements







• Definition:

The all-prefix-sums operation takes a binary associative operator  $\oplus$  with identity *I*, and an array of n elements

```
[a_{0'}, a_{1'}, \dots, a_{\underline{n}}]
```

and returns the ordered set

 $[I, a_0, (a_0 \oplus a_1), \dots, (a_0 \oplus a_1 \oplus \dots \oplus a_{n-2})].$ 

• Example:

if  $\oplus$  is addition, then scan on the set

[3 1 7 0 4 1 6 3] returns the set [0 3 4 11 11 15 16 22] Exclusive scan: last input element is not included in the result

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(From Blelloch, 1990, "Prefix EE382V: Prinicples in Computer Architecture, Fall 2008 Sums rand Their Applications) (c) Mattan Erez, 2008

# **Applications of Scan**

- Scan is a simple and useful parallel building block
  - Convert recurrences from sequential : for(j=1;j<n;j++) out[j] = out[j-1] + f(j);
  - into parallel:

```
forall(j) { temp[j] = f(j) };
scan(out, temp);
```

- Useful for many parallel algorithms:
  - radix sort
  - quicksort
  - String comparison
  - Lexical analysis
  - Stream compaction

- Polynomial evaluation
- Solving recurrences
- Tree operations
- Building data structures
- Etc.

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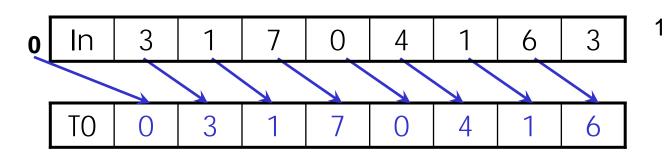


• Fun on the board

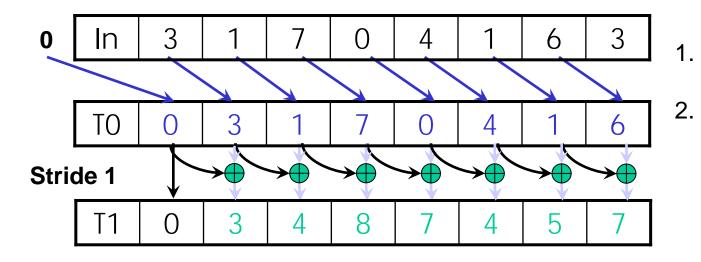
# Scan on a serial CPU

```
void scan( float* scanned, float* input, int length)
{
    scanned[0] = 0;
    for(int i = 1; i < length; ++i)
    {
        scanned[i] = input[i-1] + scanned[i-1];
    }
}</pre>
```

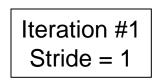
- Just add each element to the sum of the elements before it
- Trivial, but sequential
- Exactly *n* adds: optimal



Each UE reads one value from the input array in device memory into shared memory array T0. UE 0 writes 0 into shared memory array.  Read input to shared memory. Set first element to zero and shift others right by one.

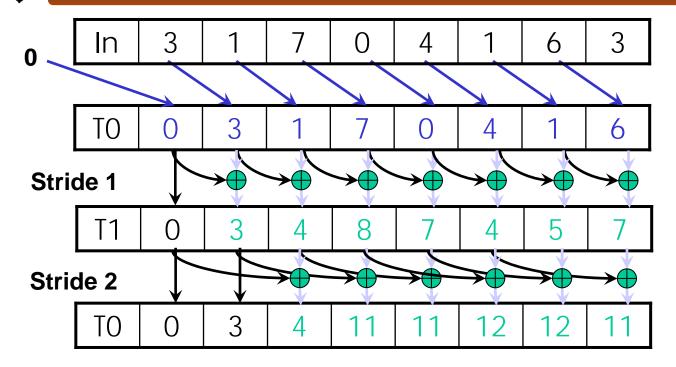


- 1. (previous slide)
  - Iterate log(n) times: UEs *stride* to *n:* Add pairs of elements s*tride* elements apart. Double *stride* at each iteration. (note must double buffer shared mem arrays)



Active UEs: stride to n-1 (n-stride UEs)
UE j adds elements j and j-stride from T0 and writes result into shared memory buffer T1 (ping-pong)

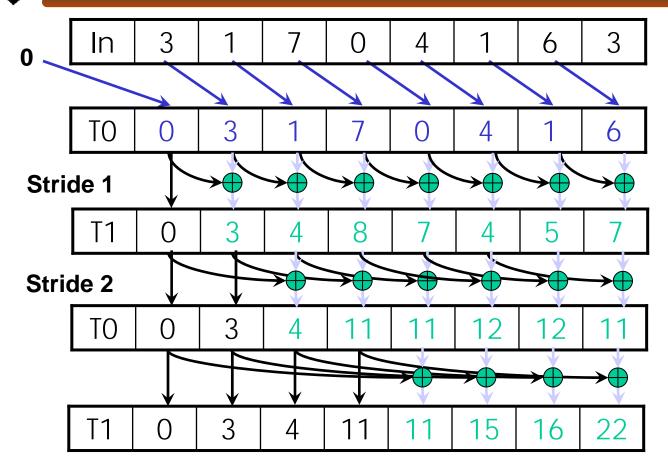
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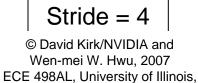
- Read input from device memory to shared memory. Set first element to zero and shift others right by one.
- Iterate log(n) times: UEs stride to n: Add pairs of elements stride elements apart. Double stride at each iteration. (note must double buffer shared mem arrays)

#### Iteration #2 Stride = 2

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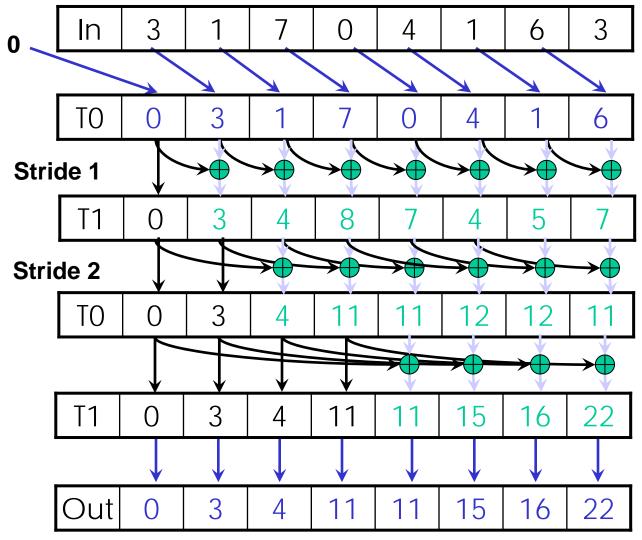


- Read input from device memory to shared memory. Set first element to zero and shift others right by one.
- Iterate log(n) times: UEs stride to n: Add pairs of elements stride elements apart. Double stride at each iteration. (note must double buffer shared mem arrays)



Iteration #3

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- Read input from device memory to shared memory. Set first element to zero and shift others right by one.
- Iterate log(n) times: UEs stride to n: Add pairs of elements stride elements apart. Double stride at each iteration. (note must double buffer shared mem arrays)
- 3. Write output.

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#### What is wrong with our first-attempt parallel scan?

- Work Efficient:
  - A parallel algorithm is work efficient if it does the same amount of work as an optimal sequential complexity
- Scan executes log(n) parallel iterations
  - The steps do n-1, n-2, n-4,... n/2 adds each
  - Total adds:  $n * (log(n) 1) + 1 \rightarrow O(n*log(n))$  work
- This scan algorithm is NOT work efficient
  - Sequential scan algorithm does *n* adds
  - A factor of log(n) hurts: 20x for 10^6 elements!



• A common parallel algorithm pattern:

#### Balanced Trees

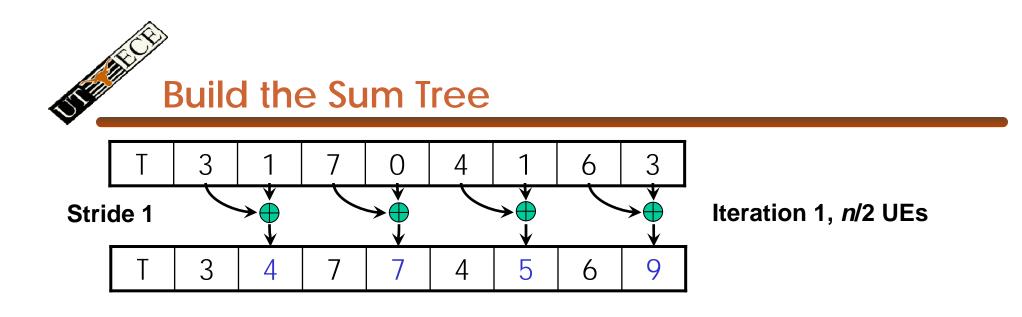
- Build a balanced binary tree on the input data and sweep it to and from the root
- Tree is not an actual data structure, but a concept to determine what each UE does at each step
- For scan:
  - Traverse down from leaves to root building partial sums at internal nodes in the tree
    - Root holds sum of all leaves
  - Traverse back up the tree building the scan from the partial sums



Assume array is already in shared memory

3

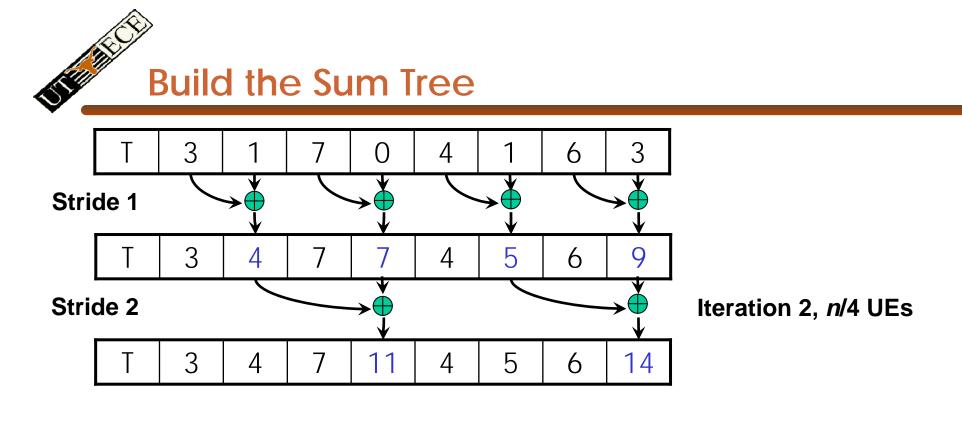
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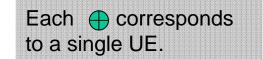




#### Iterate log(n) times. Each UE adds value *stride* elements away to its own value

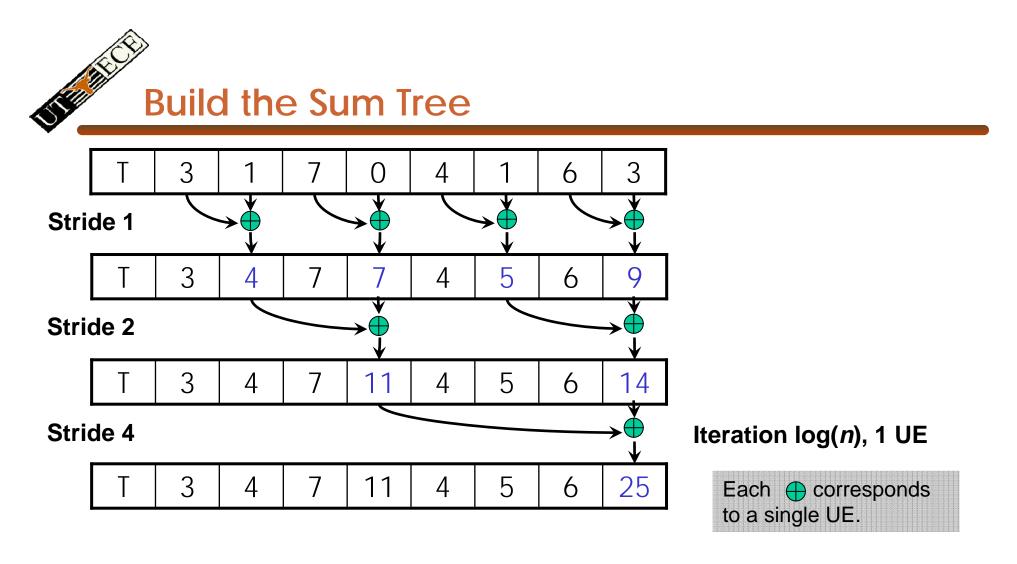
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#### Iterate log(n) times. Each UE adds value *stride* elements away to its own value

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Iterate log(n) times. Each UE adds value *stride* elements away to its own value.

Note that this algorithm operates in-place: no need for double buffering

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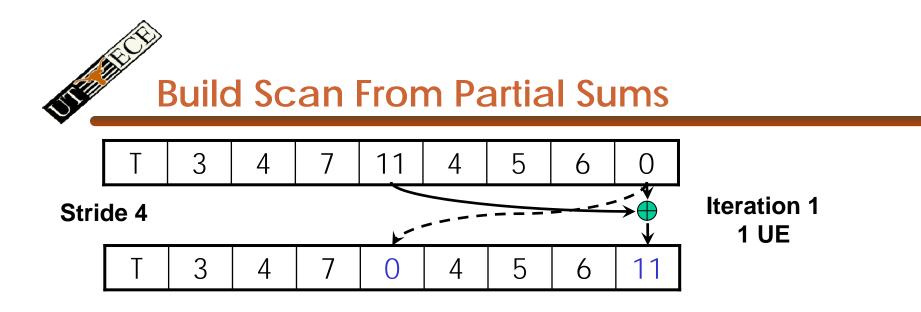


# T 3 4 7 11 4 5 6 0

We now have an array of partial sums. Since this is an exclusive scan, set the last element to zero. It will propagate back to the first element.

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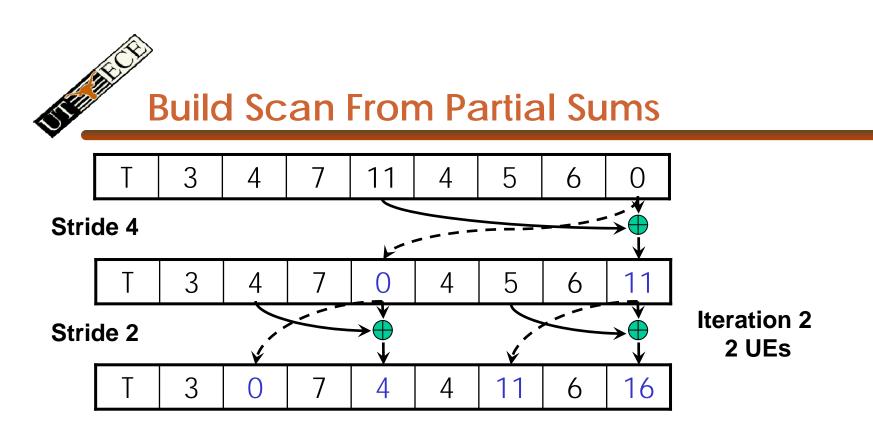




Each  $\bigoplus$  corresponds to a single UE.

Iterate log(n) times. Each UE adds value *stride* elements away to its own value, and sets the value *stride* elements away to its own *previous* value.

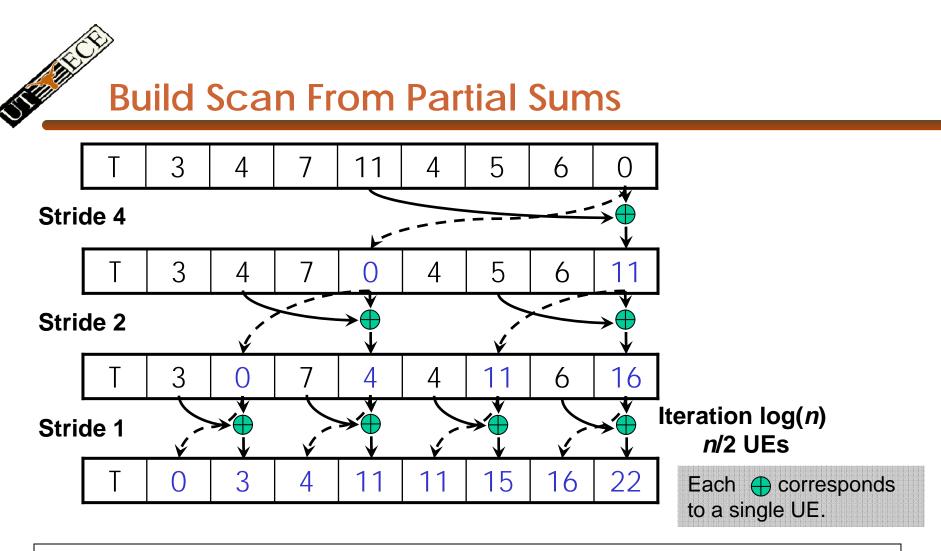
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Iterate log(n) times. Each UE adds value *stride* elements away to its own value, and sets the value *stride* elements away to its own *previous* value.

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Done! We now have a completed scan that we can write out to device memory.

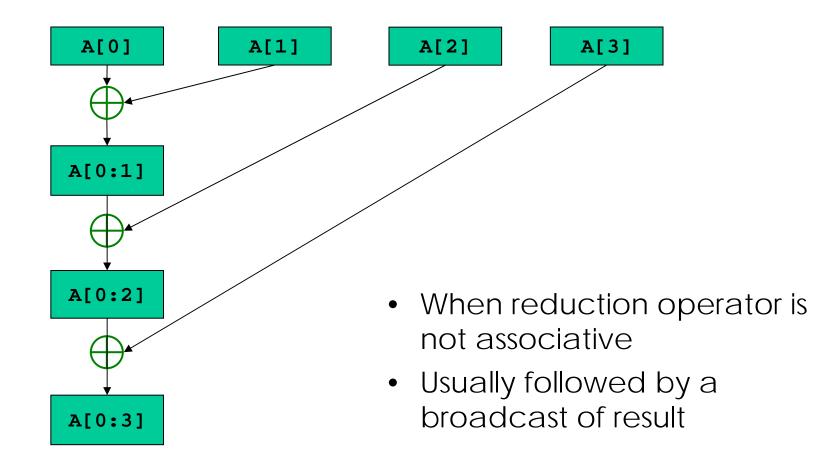
Total steps:  $2 * \log(n)$ . Total work: 2 \* (n-1) adds = O(n) Work Efficient!

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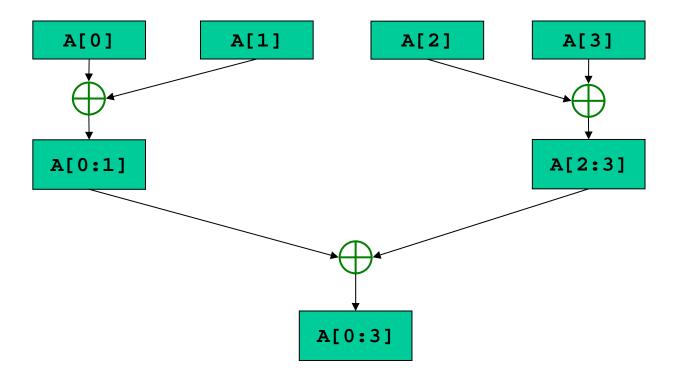


- Many to one
- Many to many
  - Simply multiple reductions
    - Also known as scatter-add and subset of parallel prefix sums
- Use
  - Histograms
  - Superposition
    - Physical properties



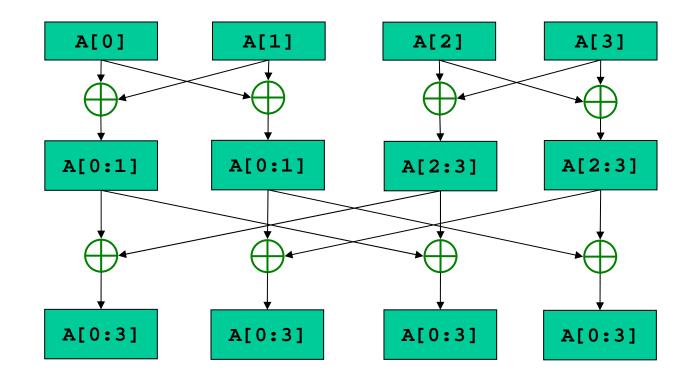






- n steps for 2<sup>n</sup> units of execution
- When reduction operator is associative
- Especially attractive when only one task needs result

**Recursive-doubling Reduction** 



- n steps for 2<sup>n</sup> units of execution
- If all units of execution need the result of the reduction

# **Recursive-doubling Reduction**

- Better than tree-based approach with broadcast
  - Each units of execution has a copy of the reduced value at the end of n steps
  - In tree-based approach with broadcast
    - Reduction takes *n* steps
    - Broadcast cannot begin until reduction is complete
    - Broadcast can take *n* steps (architecture dependent)



- More patterns
  - Reductions
  - Scans
    - Building a data structure
- More examples
  - Search
  - Sort
  - FFT as divide and conquer
  - Structured meshes and grids
  - Sparse algebra
  - Unstructured meshes and graphs
  - Trees
  - Collections
    - Particles
    - Rays

